

# Defeasible reasoning in RDFS

(Extended Abstract)

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## Abstract

For non-monotonic logics, the notion of Rational Closure (RC) is acknowledged as one of the main approaches. In this work we present an integration of RC within the triple language RDFS (Resource Description Framework Schema), which together with OWL 2 is a major standard semantic web ontology language. To do so, we start from  $\rho df$ , an RDFS fragment that covers the essential features of RDFS, and extend it to  $\rho df_{\perp}$ , allowing to state that two entities are incompatible/disjoint with each other. Eventually, we propose defeasible  $\rho df_{\perp}$  via a typical RC construction allowing to state default class/property inclusions.

## Keywords

RDFS, non-monotonic reasoning, defeasible reasoning, rational closure

## 1. Introduction

RDFS (*Resource Description Framework Schema*)<sup>1</sup> is a main standard semantic web ontology language that consists of triples  $(s, p, o)$  (denoting  $s$  is related via  $p$  with  $o$ ). The introduction of non-monotonic formalisms in reasoning with ontologies is useful in particular to deal with situations in which some classes are exceptional and do not satisfy some typical properties of their super classes, as illustrated with the following example.

**Example 1.1** (Running example). *Consider the following facts (and an intuitive translation into RDFS, where  $sc$  is read as “is a subclass of”).*

- Young people are usually happy;  $(yP, sc, hP)$
- Drug users are usually unhappy;  $(dU, sc, uhP)$
- Drug users are usually young;  $(dU, sc, yP)$
- Controlled drug users are usually happy;  $(cDU, sc, hP)$
- Controlled drug users are drug users;  $(cDU, sc, dU)$

We may consider then reasonable to conclude, for example, that controlled young drug users are usually happy.

Description Logics provide the logical foundation of formal ontologies of the semantic *Web Ontology Language* (OWL) family<sup>2</sup> and endowing them with non-monotonic features has been a main issue in the past

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<sup>1</sup><http://www.w3.org/TR/rdf-schema/>

<sup>2</sup><http://www.w3.org/TR/2009/REC-owl2-profiles-20091027>

20 years [1, 2, 3, 4, 5, 6]. On the other hand, addressing non-monotonicity in the context of RDFS, has attracted in comparison little attention so far, and almost all approaches we are aware of implement non-monotonicity by adding a so-called rule-layer on top of RDFS; see e.g., [7, 8, 9, 2, 10].

In the following, our aim is to show how to integrate Rational Closure (RC), one of the main constructions in non-monotonic reasoning [11], directly within the triple language RDFS. To do so, we start from  $\rho df$  [12, 13], a minimal, but significant RDFS fragment that covers the essential features of RDFS, and then extend it to  $\rho df_{\perp}$ , allowing to state that two entities are incompatible/disjoint with each other. The results in this paper are presented more in detail in a technical report [14].

## 2. $\rho df_{\perp}$ Graphs

We rely on a fragment of RDFS, called *minimal  $\rho df$*  [12, Def. 15], that covers all main features of RDFS, and it is essentially the formal logic behind RDFS. The vocabulary is composed by two pairwise disjoint alphabets  $\mathbf{U}$  and  $\mathbf{L}$  denoting, respectively, *URI references* and *literals*, where a literal may be a *plain literal* (e.g., a string) or a *typed literal* (e.g., a boolean value) [15]. With  $\mathbf{UL}$ , the set of *terms*, we will denote the union of these sets. A  $\rho df$ -triple is of the form  $\tau = (s, p, o) \in \mathbf{UL} \times \mathbf{U} \times \mathbf{UL}$ .<sup>3</sup> We call  $s$  the *subject*,  $p$  the *predicate*, and  $o$  the *object*. A *graph*  $G$  is a set of triples.  $\rho df$  is characterised by the set of predicates  $\{sp, sc, type, dom, range\} \subseteq \mathbf{U}$ , that can appear only as second elements in the triples. Informally, (i)  $(p, sp, q)$  means that property  $p$  is a *subproperty* of property  $q$ ; (ii)  $(c, sc, d)$  means that class  $c$  is a *subclass* of class  $d$ ; (iii)  $(a, type, b)$  means that  $a$  is of *type*  $b$ ;

<sup>3</sup>As in [12], we allow literals for  $s$ .

(iv)  $(p, \text{dom}, c)$  means that the *domain* of property  $p$  is  $c$ ; and (v)  $(p, \text{range}, c)$  means that the *range* of property  $p$  is  $c$ . We also recall that minimal  $\rho\text{df}$  does not consider so-called *blank* nodes [16, 12].

Concerning the semantics of  $\rho\text{df}$  [12], an *interpretation* is a tuple  $\mathcal{I} = \langle \Delta_R, \Delta_P, \Delta_C, \Delta_L, \mathfrak{P}[\cdot], \mathfrak{C}[\cdot], \cdot^{\mathcal{I}} \rangle$ , where  $\Delta_R, \Delta_P, \Delta_C, \Delta_L$  are the interpretation domains of  $\mathcal{I}$ , which are finite non-empty sets, and  $\mathfrak{P}[\cdot], \mathfrak{C}[\cdot], \cdot^{\mathcal{I}}$  are the interpretation functions of  $\mathcal{I}$ . In particular: (i)  $\Delta_R$  are the resources (the domain or universe of  $\mathcal{I}$ ); (ii)  $\Delta_P$  are property names (not necessarily disjoint from  $\Delta_R$ ); (iii)  $\Delta_C \subseteq \Delta_R$  are the classes; (iv)  $\Delta_L \subseteq \Delta_R$  are the literal values and contains  $\mathbf{L} \cap V$ ; (v)  $\mathfrak{P}[\cdot]$  is a function  $\mathfrak{P}[\cdot]: \Delta_P \rightarrow 2^{\Delta_R \times \Delta_R}$ ; (vi)  $\mathfrak{C}[\cdot]$  is a function  $\mathfrak{C}[\cdot]: \Delta_C \rightarrow 2^{\Delta_R}$ ; (vii)  $\cdot^{\mathcal{I}}$  maps each  $t \in \mathbf{UL} \cap V$  into a value  $t^{\mathcal{I}} \in \Delta_R \cup \Delta_P$ , and such that  $\cdot^{\mathcal{I}}$  is the identity for plain literals and assigns an element in  $\Delta_R$  to each element in  $\mathbf{L}$ .

An interpretation  $\mathcal{I}$  satisfies a graph  $G$  if for each  $(s, p, o) \in G$ ,  $p^{\mathcal{I}} \in \Delta_P$  and  $(s^{\mathcal{I}}, o^{\mathcal{I}}) \in \mathfrak{P}[p^{\mathcal{I}}]$ , and moreover  $\mathcal{I}$  satisfies a series of constraints related to the  $\rho\text{df}$ -predicates. For example, a constraint imposing that  $\mathfrak{P}[\text{sc}^{\mathcal{I}}]$  is transitive over  $\Delta_P$  indicates that the subclass relation  $\text{sc}$  must be transitive. We refer to [12, Def. 15] for the full definition of the satisfaction relation, and of the correspondent entailment relation.

**Definition 2.1** (Entailment  $\models_{\rho\text{df}}$ ). *Given two graphs  $G$  and  $H$ , we say that  $G$  entails  $H$ , denoted  $G \models_{\rho\text{df}} H$ , if and only if every model of  $G$  is also a model of  $H$ .*

In [12] the reader can find also a deduction system, consistent and complete w.r.t. the  $\rho\text{df}$  entailment relation, that is based on rules, such as

$$\frac{(A, \text{sc}, B), (B, \text{sc}, C)}{(A, \text{sc}, C)}$$

encoding the transitivity of  $\text{sc}$ .

Defeasible reasoning can be built only when faced with a conflict between the properties of a class and of a subclass. *e.g.*, in Example 1.1, “Drug users are usually unhappy” appears in conflict with “Controlled drug users are usually happy”.  $\rho\text{df}$  is not expressive enough to model such conflicts. So, we need to introduce at least a notion of incompatibility, of *disjunctiveness* [17]. Hence we enrich the  $\rho\text{df}$  vocabulary with two new predicates,  $\perp_c$  and  $\perp_p$ , representing incompatible information:  $(c, \perp_c, d)$  (resp.,  $(p, \perp_p, q)$ ) indicates that the classes  $c$  and  $d$  (resp., the properties  $p$  and  $q$ ) are disjoint. Of course we can further enrich the language allowing for logically stronger notions such as negation [18], but it is not necessary for the purpose of the present paper.

We call the new formalism, obtained by adding  $\perp_c$  and  $\perp_p$  to  $\rho\text{df}$ ,  $\rho\text{df}_{\perp}$ . Some new constraints are added to the semantics of  $\rho\text{df}$  [14, Sect. 2.2]. Here are a few examples:

- if  $(c, d) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  then  $c, d \in \Delta_C$ ;
- If  $(c, d) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$ , then  $(d, c) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  (*sc-Symmetry*);
- If  $(c, d) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  and  $(e, c) \in \mathfrak{P}[\text{sc}^{\mathcal{I}}]$ , then  $(e, d) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  (*sc-Transitivity*);
- If  $(c, c) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  and  $d \in \Delta_C$  then  $(c, d) \in \mathfrak{P}[\perp_c^{\mathcal{I}}]$  (*c-Exhaustive*).

These new constraints are such to model relevant properties of disjointedness, and allow the definition of an entailment relation  $\models_{\rho\text{df}_{\perp}}$ . An important feature of  $\rho\text{df}_{\perp}$  is also that it preserves the  $\rho\text{df}$  property that a graph is always satisfiable, avoiding the possibility of unsatisfiability and the *ex falso quodlibet* principle. This is in line with the  $\rho\text{df}$  semantics [12, 19]. From an inference system point of view, new derivation rules are added to the  $\rho\text{df}$  derivation system [14, Sect. 2.3]. The following are just a few examples:

$$\frac{(A, \perp_c, B)}{(B, \perp_c, A)} ; \quad \frac{(A, \perp_c, B), (C, \text{sc}, A)}{(C, \perp_c, B)} ; \quad \frac{(A, \perp_c, A)}{(A, \perp_c, B)} .$$

The new derivation relation  $\vdash_{\rho\text{df}_{\perp}}$  that we have defined is correct and complete w.r.t. the entailment relation  $\models_{\rho\text{df}_{\perp}}$  [14, Th. 2.1]. Eventually, we say that a graph  $G$  has a *conflict* if, for some term  $t$ , either  $G^s \vdash_{\rho\text{df}_{\perp}} (t, \perp_c, t)$  or  $G^s \vdash_{\rho\text{df}_{\perp}} (t, \perp_p, t)$  holds. The intuitive meaning is that  $G$  has a conflict if we can derive for some term  $t$  that it is either an empty class,  $(t, \perp_c, t)$ , or an empty predicate,  $(t, \perp_p, t)$ .

**Example 2.1** (Running example cont.). *In Example 1.1 we could add the triple  $(uhP, \perp_c, hP)$  to indicate that ‘being happy’ and ‘being unhappy’ are incompatible. Notice that from  $(uhP, \perp_c, hP)$ ,  $(cDU, \text{sc}, hP)$ ,  $(cDU, \text{sc}, dU)$  and  $(dU, \text{sc}, uhP)$  we conclude  $(cDU, \perp_c, cDU)$ , that is, that being a controlled drug user is incompatible with being a controlled drug user (that is,  $cDU$  should be an empty class). Analogously, from  $(uhP, \perp_c, hP)$ ,  $(dU, \text{sc}, yP)$ ,  $(yP, \text{sc}, hP)$  and  $(dU, \text{sc}, uhP)$  we conclude  $(dU, \perp_c, dU)$ .*

### 3. Defeasible $\rho\text{df}_{\perp}$

Next we show how to model defeasible information. Here we consider defeasibility w.r.t. the predicates  $\text{sc}$  and  $\text{sp}$  only, and introduce the notion of *defeasible triple*:

$$\delta = \langle s, p, o \rangle \in \mathbf{UL} \times \{\text{sc}, \text{sp}\} \times \mathbf{UL} ,$$

where  $s, o \notin \rho\text{df}_{\perp}$ . The intended meaning of *e.g.*,  $\langle c, \text{sc}, d \rangle$  is “Typically, an instance of  $c$  is also an instance of  $d$ ”. Analogously,  $\langle p, \text{sp}, q \rangle$  is read as “Typically, a pair related by  $p$  is also related by  $q$ ”.

**Example 3.1** (Running example cont.). In Example 1.1 the statements containing ‘usually’ can more correctly be modelled using defeasible triples, that is,  $\langle yP, \text{sc}, hP \rangle$ ,  $\langle dU, \text{sc}, uhP \rangle$ ,  $\langle dU, \text{sc}, yP \rangle$  and  $\langle cDU, \text{sc}, hP \rangle$ .

There are various ways of reasoning in a defeasible framework. Here we take under consideration RC [11], since, despite having some limits from the inferential point of view [20], it is a main inference relation in conditional reasoning on top of which we can define other interesting forms of entailment [20, 21, 22].

We give here only a short overview of the reasoning procedure, inviting the reader to check [14] for a comprehensive presentation. Given a defeasible graph  $G$  and a query  $\langle s, p, o \rangle$ , we decide whether  $\langle s, p, o \rangle$  is in the RC of  $G$  through a two-step procedure:

1. We rank all the defeasible triples in  $G$ , considering the potential conflicts and the relative logical specificity of the first elements of the triples. We give priority (that is, a higher rank) to more specific triples. To check the presence of potential conflicts in a graph, we translate all the defeasible triples into the correspondent  $\text{pdf}_\perp$  triples, that is, we create a new  $\text{pdf}_\perp$  graph in which every defeasible  $\langle s, p, o \rangle$  is substituted by  $\langle s, p, o \rangle$ .

**Example 3.2** (Running example cont.). In Example 2.1 we have seen that from the  $\text{pdf}_\perp$  version of our graph we obtain  $\langle cDU, \perp_c, cDU \rangle$  and  $\langle dU, \perp_c, dU \rangle$ . From this we conclude that all the defeasible triples with  $cDU$  or  $dU$  as first element (e.g.,  $\langle cDU, \text{sc}, hP \rangle$  and  $\langle dU, \text{sc}, uhP \rangle$ ) have priority (a higher rank) w.r.t. the other defeasible triples. That is,  $\langle yP, \text{sc}, hP \rangle$  has rank 0, while the other defeasible triples are exceptional. We then reiterate the procedure considering only the exceptional triples and the  $\text{pdf}_\perp$ -triples, that is,  $\{\langle dU, \text{sc}, uhP \rangle, \langle dU, \text{sc}, yP \rangle, \langle cDU, \text{sc}, hP \rangle\} \cup \{\langle cDU, \text{sc}, dU \rangle, \langle hP, \perp_c, uhP \rangle\}$ . Translating the defeasible triples into  $\text{pdf}_\perp$ -triples, the only conflict we can still derive is  $\langle cDU, \perp_c, cDU \rangle$ , hence we have that  $\langle dU, \text{sc}, uhP \rangle, \langle dU, \text{sc}, yP \rangle$  have rank 1, while  $\langle cDU, \text{sc}, hP \rangle$  is exceptional. From  $\{\langle cDU, \text{sc}, hP \rangle\} \cup \{\langle cDU, \text{sc}, dU \rangle, \langle hP, \perp_c, uhP \rangle\}$  we cannot derive anymore  $\langle cDU, \perp_c, cDU \rangle$ , hence  $\langle cDU, \text{sc}, hP \rangle$  has rank 2 and we have finished the ranking of the graph.

Note that, given a graph  $G$ , the ranking procedure needs to be done once and for all.

2. Given a query  $\langle s, \text{sc}, o \rangle$  (resp.,  $\langle s, \text{sp}, o \rangle$ ), we check the rank of  $s$ , i.e., we check which is the lowest rank in which we do not derive  $\langle s, \perp_c, s \rangle$  (resp.,  $\langle s, \perp_p, s \rangle$ ), and then we check whether we can derive  $\langle s, \text{sc}, o \rangle$  (resp.,  $\langle s, \text{sp}, o \rangle$ ) considering only the defeasible triples with at least such a rank.

**Example 3.3** (Running example cont.). We wonder whether  $\langle cDU, \text{sc}, uhP \rangle$  is in the RC of our graph. This triple is interesting because it would be derivable in the monotonic  $\text{pdf}_\perp$ -graph we have considered up to Example 2.1, but it is undesirable since we are aware that  $\langle cDU, \text{sc}, hP \rangle$  and that ‘Drug users are usually happy’, that is a defeasible statement. If we consider our entire graph, we already know (Example 3.2) that  $cDU$  is exceptional, that is, substituting the defeasible triples with their  $\text{pdf}_\perp$  counterparts, we obtain  $\langle cDU, \perp_c, cDU \rangle$ . The same if we consider the graph obtained eliminating all the defeasible triples of rank 0. Only once we eliminate also the triples of rank 1, and we consider only the graph  $\{\langle cDU, \text{sc}, hP \rangle\} \cup \{\langle cDU, \text{sc}, dU \rangle, \langle hP, \perp_c, uhP \rangle\}$ , we are not able to derive  $\langle cDU, \perp_c, cDU \rangle$  anymore. That is, we do not have a conflict anymore on  $cDU$ . Our query  $\langle cDU, \text{sc}, uhP \rangle$  will be decided considering only this portion of the original graph:  $\{\langle cDU, \text{sc}, hP \rangle\} \cup \{\langle cDU, \text{sc}, dU \rangle, \langle hP, \perp_c, uhP \rangle\}$ . In order to decide whether  $\langle cDU, \text{sc}, uhP \rangle$ , we check whether its  $\text{pdf}_\perp$ -counterpart,  $\langle cDU, \text{sc}, uhP \rangle$ , is derivable from the  $\text{pdf}_\perp$ -counterpart of the portion of the graph we consider; that is,  $\{\langle cDU, \text{sc}, hP \rangle, \langle cDU, \text{sc}, dU \rangle, \langle hP, \perp_c, uhP \rangle\}$ . It is easy to check that there is no way of deriving  $\langle cDU, \text{sc}, uhP \rangle$  from this graph.

The semantics for defeasible  $\text{pdf}_\perp$  are defined with a ranking of  $\text{pdf}_\perp$ -models: the lowest the rank of the model, the more expected the situation it describes is considered. As for the propositional and DL case [23], given a defeasible graph  $G$  its RC is determined by its *minimal* ranked model, that is, the model of  $G$  in which every  $\text{pdf}_\perp$ -model is ranked as low as possible. The technical details can be found in [14, Sect. 3].

## 4. Conclusions

The main features of our approach are: (i) the defeasible  $\text{pdf}_\perp$  we propose remains syntactically a triple language by extending it with new predicate symbols with specific semantics; (ii) the logic is defined in such a way that any RDFS reasoner/store may handle the new predicates as ordinary terms if it does not want to take into account of the extra non-monotonic capabilities; (iii) the defeasible entailment decision procedure is built on top of the  $\text{pdf}_\perp$  entailment decision procedure, which in turn is an extension of the one for  $\text{pdf}$  via some additional inference rules, favouring a potential implementation; (iv) the computational complexity of deciding entailment in  $\text{pdf}$  and  $\text{pdf}_\perp$  are the same; and (v) defeasible entailment can be decided via a polynomial number of calls to an oracle deciding ground triple entailment in  $\text{pdf}_\perp$  and, in particular, deciding defeasible entailment can be done in polynomial time. While an extended version of the paper is under review at the moment, a technical report is online [14].

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